ES 250 Practice Final Exam

1. Given that

$$
v_{\mathrm{a}}=8 \mathrm{~V},
$$

Determine the values of $R_{1}$ and $v_{\mathrm{o}}$ :

$$
R_{1}=\_10 \_\Omega,
$$

and

$$
v_{\mathrm{o}}=\_-3.2 \_\mathrm{V}
$$

$4 \Omega$

10 V

$v_{\mathrm{a}}=20 i_{\mathrm{b}}$
2. Given that $0 \leq R \leq \infty$ in this circuit, consider these two observations:
When $R=2 \Omega$ then $v_{\mathrm{R}}=4 \mathrm{~V}$ and $i_{\mathrm{R}}=2 \mathrm{~A}$.
When $R=6 \Omega$ then $v_{\mathrm{R}}=6 \mathrm{~V}$ and $i_{\mathrm{R}}=1 \mathrm{~A}$.
Fill in the blanks in the following statements:

a. The maximum value of $i_{\mathrm{R}}$ is $\qquad$ 4 $\qquad$ A.
b. The maximum value of $v_{\mathrm{R}}$ is $\qquad$ 8 $\qquad$ V.
c. The maximum value of $p_{\mathrm{R}}=i_{\mathrm{R}} v_{\mathrm{R}}$ occurs when $R=$ $\qquad$ 2 $\qquad$ $\Omega$.
d. The maximum value of $p_{\mathrm{R}}=i_{\mathrm{R}} v_{\mathrm{R}}$ is $\qquad$ 8 $\qquad$ W.
3.



The input to this circuit is the voltage, $v_{\mathrm{s}}$. The output is the voltage $v_{\mathrm{o}}$. The voltage $v_{\mathrm{b}}$ is used to adjust the relationship between the input and output. Determine values of $R_{4}$ and $v_{\mathrm{b}}$ that cause the circuit input and output have the relationship specified by the graph
$v_{\mathrm{b}}=$ $\qquad$ .62 $\qquad$ V and $R_{4}=$ $\qquad$ 62.5 $\qquad$ $\mathrm{k} \Omega$.
4. Consider this inductor. The current and voltage are given by

$$
i(t)=\left\{\begin{array}{cc}
5 t-4.6 & 0 \leq t \leq 0.2 \\
a t+b & 0.2 \leq t \leq 0.5 \\
c & t \geq 0.5
\end{array} \text { and } \quad v(t)=\left\{\begin{array}{ccc}
12.5 & 0<t<0.2 \\
25 & 0.2<t<0.5 \\
0 & t>0.5
\end{array} \quad v(t)\{L=2.5 \mathrm{H}\right.\right.
$$

where $\mathrm{a}, \mathrm{b}$ and c are real constants. (The current is given in Amps, the voltage in Volts and the time in seconds.) Determine the values of the constants:

$$
a=\_10 \_\_\mathrm{A} / \mathrm{s}, \quad b=\_-5.6 \ldots \mathrm{~A} \text { and } c=\_-0.6 \_\mathrm{A}
$$

5. This circuit is at steady state when the switch opens at time $t=0$.


The capacitor voltage is $v(t)=A+B e^{-a t}$ for $t \geq 0$. Determine the values of the constants $A, B$, and $a$ :

$$
A=\_4 \_\mathrm{V}, \quad B=\_8 \_\_\mathrm{V} \text { and } a=\_\quad 10 \_\mathrm{s} .
$$

6. This circuit is at steady state before the switch closes at time $t=0$. After the switch closes, the inductor current is given by

$$
i(t)=0.6-0.2 e^{-5 t} \quad \mathrm{~A} \quad \text { for } t \geq 0
$$

Determine the values of $R_{1}, R_{2}$ and $L$ :

$$
R_{1}=\_20 \_\Omega, R_{2}=\_10 \_\Omega
$$


and

$$
L=\_4 \_\mathrm{H}
$$

7. The voltage and current for this circuit are given by

$$
v(t)=20 \cos \left(20 t+15^{\circ}\right) \mathrm{V} \quad \text { and } \quad i(t)=1.49 \cos \left(20 t+63^{\circ}\right) \mathrm{A}
$$

Determine the values of the resistance, $R$, and capacitance, $C$ :

$$
R=\_\quad 9 \_\Omega \text { and } C=\_5 \quad \mathrm{mF} .
$$


8.


This circuit is at steady state. The voltage source voltages are given by

$$
v_{1}(t)=12 \cos \left(2 t-90^{\circ}\right) \mathrm{V} \text { and } v_{2}(t)=5 \cos \left(2 t+90^{\circ}\right) \mathrm{V}
$$

The currents are given by

$$
i_{1}(t)=744 \cos \left(2 t-118^{\circ}\right) \mathrm{mA}, i_{2}(t)=540.5 \cos \left(2 t+100^{\circ}\right) \mathrm{mA} \text { and } i(t)=A \cos \left(2 t-164^{\circ}\right) \mathrm{mA}
$$

Determine the values of $A, R_{1}, R_{2}, L$ and $C$ :

$$
A=\_460 \_\mathrm{mA}, R_{1}=\_10 \_\Omega, R_{2}=\_10 \_\Omega, L=\_6 \_\mathrm{H} \text { and } C=\_50 \_\mathrm{mF} \text {. }
$$

9. The input this circuit is the current

$$
i_{\mathrm{s}}(t)=2 \cos \left(5 t+15^{\circ}\right) \mathrm{A} .
$$

In the frequency domain, this circuit is represented by the node equation

$$
\left[\begin{array}{cc}
d+j 0.5 & -j 0.5 \\
-j 0.5 & 0.25+j e
\end{array}\right]\left[\begin{array}{l}
\mathbf{V}_{\mathrm{a}} \\
\mathbf{V}_{\mathrm{b}}
\end{array}\right]=\left[\begin{array}{c}
2 \angle 15^{\circ} \\
0
\end{array}\right]
$$


where $\mathbf{V}_{\mathrm{a}}$ and $\mathbf{V}_{\mathrm{b}}$ are the phasor node voltages and $d$ and $e$ are real numbers. Determine the values of $d$ and $e$.

$$
d=\_0.125 \_\Omega \text { and } e=\_-3.5 \_\Omega
$$

