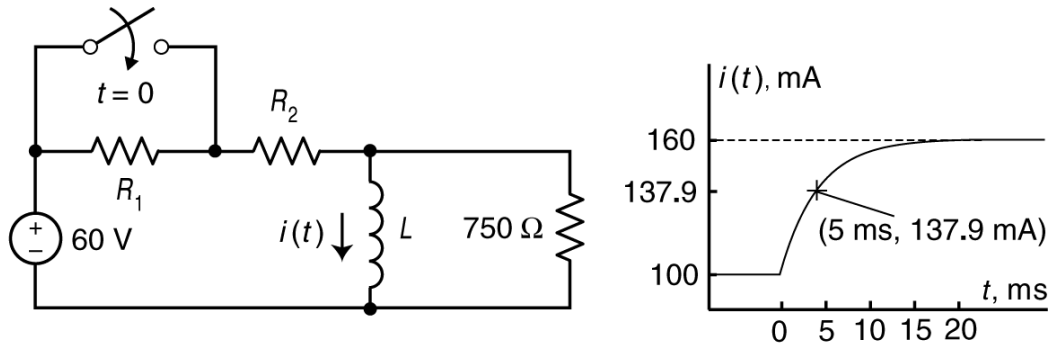


## EE221 1<sup>st</sup> Midterm Exam - Spring 2014

Name \_\_\_\_\_

Student # \_\_\_\_\_

1.

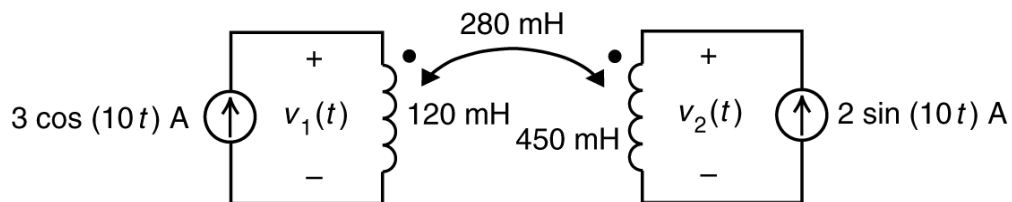


Determine the values of  $R_1$  and  $R_2$ .

$$R_1 = \underline{\quad 225 \quad} \Omega \text{ and } R_2 = \underline{\quad 375 \quad} \Omega.$$

b. Determine the value of the time constant,  $\tau$ , of this circuit after the switch closes:  $\tau = \underline{\quad 5 \quad}$  ms.

2.



(Recall that  $\sin(\omega t) = \cos(\omega t - 90^\circ)$ .) The coil voltages in this circuit are  $v_1(t) = A \cos(10t + 32.74^\circ)$  V and  $v_2(t) = B \cos(10t + 43.03^\circ)$  V. Determine the values of  $A$  and  $B$ :

$$A = \underline{\quad 6.657 \quad} \text{ V and } B = \underline{\quad 12.311 \quad} \text{ V}$$

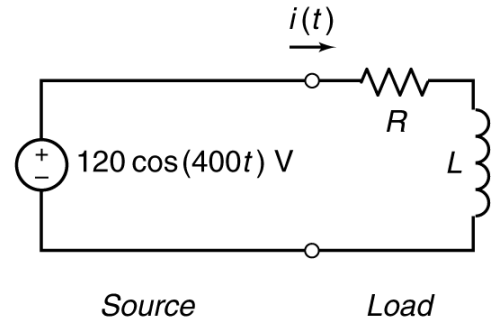
3. An AC source is connected to a load:

a) Suppose that the voltage source supplies

$$\mathbf{S} = 10.186 \angle 25.11^\circ = 9.2234 + j 4.3225 \text{ VA}$$

Determine values of the resistance and inductance.

$$R = \underline{\quad 640 \quad} \Omega \quad \text{and} \quad L = \underline{\quad 750 \quad} \text{mH}$$



b) Suppose **instead** that  $i(t) = 191 \cos(400t - 37.2^\circ)$  mA . Determine the values of the real and reactive powers supplied by the source to the load.

$$P = \underline{\quad 9.13 \quad} \text{ W} \quad \text{and} \quad Q = \underline{\quad 6.93 \quad} \text{ VAR}$$

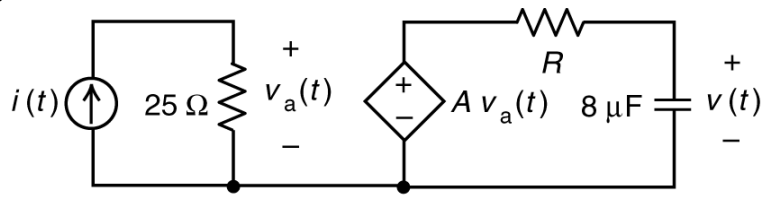
c) Suppose **instead** that  $R = 500 \Omega$  and  $L = 600 \text{ mH}$ . Determine the power factor of the load:

$$pf = \underline{\quad 0.9015 \quad}$$

d) Suppose **instead** that the voltage source supplies 7.067 W at a power factor of 0.817 lagging. Determine the values of the apparent and reactive powers supplied by the source to the load.

$$|\mathbf{S}| = \underline{\quad 8.65 \quad} \text{ VA} \quad \text{and} \quad Q = \underline{\quad 4.99 \quad} \text{ VAR}$$

4.



The network function of this circuit is:

$$\mathbf{H}(\omega) = \frac{\mathbf{V}(\omega)}{\mathbf{I}(\omega)} = \frac{800}{1 + j \frac{\omega}{500}}$$

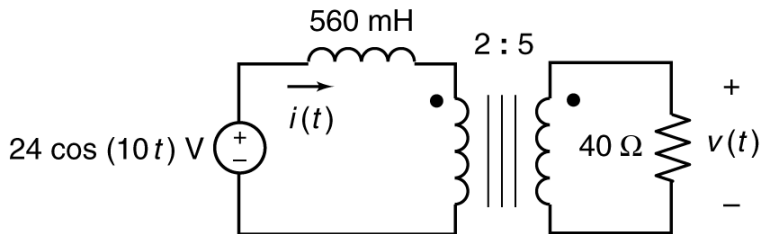
- a) The value of the resistance is  $R = \underline{250} \Omega$ .
- b) The value of the gain of the VCVS is  $A = \underline{32} \text{ V/A}$ .
- c) When  $\omega = 400 \text{ rad/sec}$ , the value of the gain of the circuit is  $\underline{624.7} \text{ V/A}$ .
- d) When  $\omega = 400 \text{ rad/sec}$ , the value of the phase shift of the circuit is  $\underline{-38.7}^\circ$ .
- e) When  $\omega = \underline{866} \text{ rad/sec}$ , the value of the gain of the circuit is  $400 \text{ V/V}$ .
- f) When  $\omega = \underline{287} \text{ rad/sec}$ , the value of the phase shift of the circuit is  $-30^\circ$ .
- g) At low frequencies the value of the gain of the circuit is  $\underline{800} \text{ V/A}$ .
- h) At high frequencies the value of the phase shift of the circuit is  $\underline{-90}^\circ$ .
- i) When the input is  $i(t) = 180 \cos(300t + 15^\circ) \text{ mA}$  the amplitude of  $v(t)$  is  $\underline{123.5} \text{ V}$ .
- j) When the input is  $i(t) = 180 \cos(300t + 15^\circ) \text{ mA}$  the phase angle of  $v(t)$  is  $\underline{-16}^\circ$ .

5. The current  $i(t)$  and voltage  $v(t)$  labeled on the circuit drawing are

$$i(t) = A \cos(10t - 41.19^\circ) \text{ Amps}$$

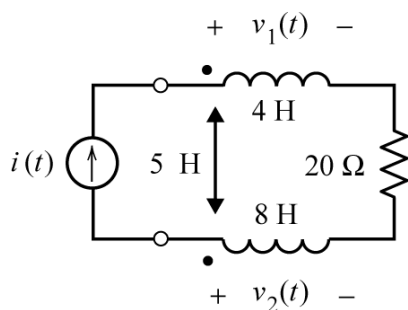
and  $v(t) = B \cos(10t - 41.19^\circ) \text{ V}$

Determine the values of  $A$  and  $B$ :



$$A = \underline{\quad 2.822 \quad} \text{ Amps} \quad \text{and} \quad B = \underline{\quad 45.15 \quad} \text{ V}$$

6.



The input current is

$$i(t) = 1.3 \cos(6t) \text{ A}$$

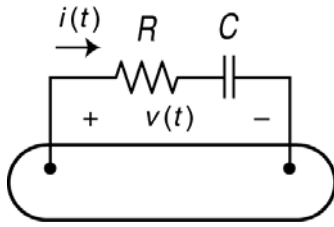
The coil voltages are

$$v_1(t) = E \cos(6t - 90^\circ) \text{ V} \quad \text{and} \quad v_2(t) = F \cos(6t - 90^\circ) \text{ V}$$

Determine the values of  $E$  and  $F$ .

$$E = \underline{\quad 7.8 \quad} \text{ V} \quad \text{and} \quad F = \underline{\quad 23.4 \quad} \text{ V}$$

7.



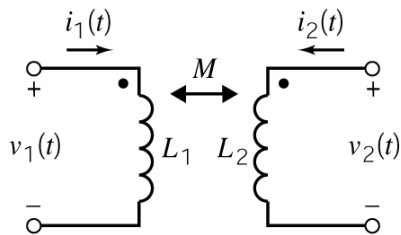
This voltage and current are given by

$$v(t) = 15 \cos(20t + 40^\circ) \text{ V} \quad \text{and} \quad i(t) = 1.59 \cos(20t + 72^\circ) \text{ A}$$

Determine the values of the resistance,  $R$ , and capacitance,  $C$ .

$$R = \underline{\quad 8 \quad} \Omega \quad \text{and} \quad C = \underline{\quad 10 \quad} \text{mF}$$

QUANTITY	RELATIONSHIP USING PEAK VALUES	RELATIONSHIP USING rms VALUES	UNITS
Element voltage, $v(t)$	$v(t) = V_m \cos(\omega t + \theta_v)$	$v(t) = V_{\text{rms}} \sqrt{2} \cos(\omega t + \theta_v)$	V
Element current, $i(t)$	$i(t) = I_m \cos(\omega t + \theta_i)$	$i(t) = I_{\text{rms}} \sqrt{2} \cos(\omega t + \theta_i)$	A
Complex power, $\mathbf{S}$	$\mathbf{S} = \frac{V_m I_m}{2} \cos(\theta_v - \theta_i)$ $+ j \frac{V_m I_m}{2} \sin(\theta_v - \theta_i)$	$\mathbf{S} = V_{\text{rms}} I_{\text{rms}} \cos(\theta_v - \theta_i)$ $+ j V_{\text{rms}} I_{\text{rms}} \sin(\theta_v - \theta_i)$	VA
Apparent power, $ \mathbf{S} $	$ \mathbf{S}  = \frac{V_m I_m}{2}$	$ \mathbf{S}  = V_{\text{rms}} I_{\text{rms}}$	VA
Average power, $P$	$P = \frac{V_m I_m}{2} \cos(\theta_v - \theta_i)$	$P = V_{\text{rms}} I_{\text{rms}} \cos(\theta_v - \theta_i)$	W
Reactive power, $Q$	$Q = \frac{V_m I_m}{2} \sin(\theta_v - \theta_i)$	$Q = V_{\text{rms}} I_{\text{rms}} \sin(\theta_v - \theta_i)$	VAR

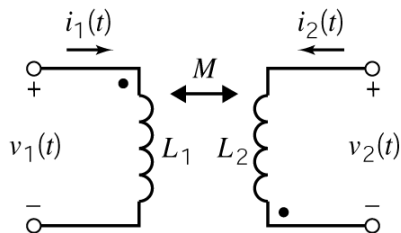


$$v_1 = L_1 \frac{di_1}{dt} + M \frac{di_2}{dt}$$

$$\mathbf{V}_1 = j\omega L_1 \mathbf{I}_1 + j\omega M \mathbf{I}_2$$

$$v_2 = L_2 \frac{di_2}{dt} + M \frac{di_1}{dt}$$

$$\mathbf{V}_2 = j\omega L_2 \mathbf{I}_2 + j\omega M \mathbf{I}_1$$

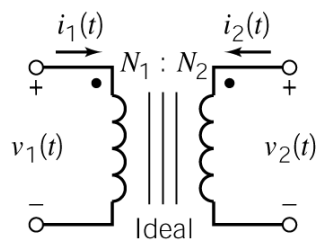


$$v_1 = L_1 \frac{di_1}{dt} - M \frac{di_2}{dt}$$

$$\mathbf{V}_1 = j\omega L_1 \mathbf{I}_1 - j\omega M \mathbf{I}_2$$

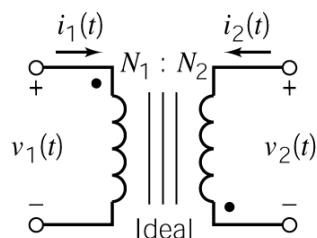
$$v_2 = L_2 \frac{di_2}{dt} - M \frac{di_1}{dt}$$

$$\mathbf{V}_2 = j\omega L_2 \mathbf{I}_2 - j\omega M \mathbf{I}_1$$



$$\mathbf{V}_1 = \frac{N_1}{N_2} \mathbf{V}_2$$

$$\mathbf{I}_1 = -\frac{N_2}{N_1} \mathbf{I}_2$$



$$\mathbf{V}_1 = -\frac{N_1}{N_2} \mathbf{V}_2$$

$$\mathbf{I}_1 = \frac{N_2}{N_1} \mathbf{I}_2$$