## EE221 $1^{\text {st }}$ Midterm Exam - Spring 2014

Name $\qquad$ Student \# $\qquad$
1.



Determine the values of $R_{1}$ and $R_{2}$.

$$
R_{1}=
$$

$\qquad$ 90 $\qquad$ $\Omega$ and $R_{2}=$ $\qquad$ 150 $\qquad$ $\Omega$.
b. Determine the value of the time constant, $\tau$, of the this circuit after the switch closes: $\tau=$ $\qquad$ _5 $\qquad$ ms.
2.

(Recall that $\sin (\omega t)=\cos \left(\omega t-90^{\circ}\right)$.) The coil voltages in this circuit are $v_{1}(t)=A \cos \left(10 t+15.95^{\circ}\right) \mathrm{V}$ and $v_{2}(t)=B \cos \left(10 t+22.53^{\circ}\right) \mathrm{V}$. Determine the values of $A$ and $B$ :

$$
A=\ldots 8.736 \quad \mathrm{~V} \text { and } B=\ldots \quad 14.615 \_\quad \mathrm{V}
$$

3. An AC source is connected to a load:
a) Suppose that the voltage source supplies

$$
\mathbf{S}=9.1 \angle 24.49^{\circ}=8.2814+j 3.7723 \mathrm{VA}
$$

Determine values of the resistance and inductance.

$$
R=\_720 \_\Omega \text { and } L=\_820 \_\mathrm{mH}
$$

Source
b) Suppose instead that $R=420 \Omega$ and $L=800 \mathrm{mH}$. Determine the power factor of the load:

$$
p f=\_0.7954 \_
$$

c) Suppose instead that the voltage source supplies 9.1278 W at a power factor of 0.7962 lagging. Determine the values of the apparent and reactive powers supplied by the source to the load.

$$
|\mathbf{S}|=\_\quad 11.464 \_ \text {VA and } Q=\ldots 6.936 \_ \text {VAR }
$$

d) Suppose instead that $i(t)=176.47 \cos \left(400 t-28.1^{\circ}\right) \mathrm{mA}$. Determine the values of the real and reactive powers supplied by the source to the load.

$$
P=\_\quad 9.34 \_\mathrm{W} \text { and } Q=\_4.98 \_ \text {VAR }
$$

4. 



The network function of this circuit is:

$$
\mathbf{H}(\omega)=\frac{\mathbf{V}(\omega)}{\mathbf{I}(\omega)}=\frac{450}{1+j \frac{\omega}{250}}
$$

a) The value of the resistance is $R=$ $\qquad$ 500 $\qquad$ $\Omega$.
b) The value of the gain of the VCVS is $A=$ $\qquad$ 18 $\qquad$ V/V.
c) When $\omega=$ $\qquad$ 433 ra $\mathrm{rad} / \mathrm{sec}$, the value of the gain of the circuit is $225 \mathrm{~V} / \mathrm{A}$.
d) When $\omega=$ $\qquad$ $144 \_\mathrm{rad} / \mathrm{sec}$, the value of the phase shift of the circuit is $-30^{\circ}$.
e) When $\omega=200 \mathrm{rad} / \mathrm{sec}$, the value of the gain of the circuit is $\qquad$ 351 $\qquad$ V/A.
f) When $\omega=200 \mathrm{rad} / \mathrm{sec}$, the value of the phase shift of the circuit is $\qquad$ $-38.7 \ldots{ }^{\circ}$.
g) At low frequencies the value of the gain of the circuit is $\qquad$ 450 $\qquad$ V/A.
h) At high frequencies the value of the phase shift of the circuit is $\qquad$ $-90$ $\qquad$ ${ }^{\circ}$.
i) When the input is $i(t)=180 \cos \left(300 t+30^{\circ}\right) \mathbf{m A}$ the phase angle of $v(t)$ is $\qquad$ $-20.2 ـ^{\circ}$.
j) When the input is $i(t)=180 \cos \left(300 t+30^{\circ}\right) \mathbf{m A}$ the amplitude of $v(t)$ is $\qquad$ 51.85 $\qquad$ V.
5. The current $i(t)$ and voltage $v(t)$ labeled on the circuit drawing are

$$
i(t)=A \cos \left(10 t-23.63^{\circ}\right) \mathrm{Amps}
$$

and $\quad v(t)=B \cos \left(10 t-23.63^{\circ}\right) \mathrm{V}$
Determine the values of $A$ and $B$ :


$$
A=
$$

$\qquad$ 1.718 $\qquad$ Amps and $B=$ $\qquad$ 54.97 $\qquad$ V
6.


The input current is

$$
i(t)=1.3 \cos (5 t) \mathrm{A}
$$

The coil voltages are

$$
v_{1}(t)=E \cos \left(5 t-90^{\circ}\right) \mathrm{V} \quad \text { and } \quad v_{2}(t)=F \cos \left(5 t-90^{\circ}\right) \mathrm{V}
$$

Determine the values of $E$ and $F$.

$$
E=\_6.5 \_\mathrm{V} \text { and } F=\_19.5 \_\mathrm{V}
$$

7. 

This voltage and current are given by

$$
v(t)=20 \cos \left(25 t+15^{\circ}\right) \mathrm{V} \text { and } i(t)=3.05 \cos \left(25 t+39^{\circ}\right) \mathrm{A}
$$

Determine the values of the resistance, $R$, and capacitance, $C$.

$$
R=\ldots \quad 6 \quad \Omega \text { and } C=\ldots 15 \ldots \mathrm{~m} \mathrm{~F}
$$

| QUANTITY | RELATIONSHIP USING PEAK VALUES | RELATIONSHIP USING rms VALUES | UNITS |
| :---: | :---: | :---: | :---: |
| Element voltage, $v(t)$ | $v(t)=V_{\mathrm{m}} \cos \left(\omega t+\theta_{\mathrm{v}}\right)$ | $v(t)=V_{\text {rms }} \sqrt{2} \cos \left(\omega t+\theta_{\mathrm{V}}\right)$ | V |
| Element current, $i(t)$ | $i(t)=I_{\mathrm{m} \cos \left(\omega t+\theta_{\mathrm{I}}\right)}$ | $i(t)=V_{\mathrm{rms}} \sqrt{2} \cos \left(\omega t+\theta_{\mathrm{I}}\right)$ | A |
| Complex power, S | $\mathbf{S}=\frac{V_{\mathrm{m}} I_{\mathrm{m}}}{2} \cos \left(\theta_{\mathrm{v}}-\theta_{\mathrm{I}}\right)$ | $\mathbf{S}=V_{\text {rms }} I_{\text {rms }} \cos \left(\theta_{\mathrm{V}}-\theta_{\mathrm{I}}\right)$ | VA |
|  | $+j \frac{V_{\mathrm{m}} I_{\mathrm{m}}}{2} \sin \left(\theta_{\mathrm{v}}-\theta_{\mathrm{I}}\right)$ | $+j V_{\mathrm{rms}} I_{\mathrm{rms}} \sin \left(\theta_{\mathrm{V}}-\theta_{\mathrm{I}}\right)$ |  |
| Apparent power, \|S| | $\|\mathbf{S}\|=\frac{V_{\mathrm{m}} I_{\mathrm{m}}}{2}$ | $\|\mathbf{S}\|=V_{\text {rms }} I_{\text {rms }}$ | VA |
| Average power, $P$ | $P=\frac{V_{\mathrm{m}} I_{\mathrm{m}}}{2} \cos \left(\theta_{\mathrm{v}}-\theta_{\mathrm{I}}\right)$ | $P=V_{\mathrm{rms}} I_{\mathrm{rms}} \cos \left(\theta_{\mathrm{V}}-\theta_{\mathrm{I}}\right)$ | W |
| Reactive power, $Q$ | $Q=\frac{V_{\mathrm{m}} I_{\mathrm{m}}}{2} \sin \left(\theta_{\mathrm{v}}-\theta_{\mathrm{I}}\right)$ | $Q=V_{\mathrm{rms}} I_{\mathrm{rms}} \sin \left(\theta_{\mathrm{V}}-\theta_{\mathrm{I}}\right)$ | VAR |
|  | $i_{2}(t)$ |  |  |
|  | $\longleftarrow_{+}^{\infty} \quad v_{1}=L_{1} \frac{d i_{1}}{d t}$ | $M \frac{d i_{2}}{d t} \quad \mathbf{V}_{1}=j \omega L_{1} \mathbf{l}_{1}+$ |  |
|  | $\mathrm{c}_{-}^{v_{2}(t)} \quad v_{2}=L_{2} \frac{d i_{2}}{d t}$ | $M \frac{d i_{1}}{d t} \quad \mathbf{V}_{2}=j \omega L_{2} \mathbf{I}_{2}+$ |  |
|  | $\stackrel{i_{2}(t)}{\overbrace{+}} \quad v_{1}=L_{1} \frac{d i_{1}}{d t}$ |  |  |
|  | $\begin{gathered} v_{2}(t) \\ - \\ v_{2}=L_{2} \frac{d i_{2}}{d t} \end{gathered}$ | $M \frac{d i_{1}}{d t} \quad \mathbf{V}_{2}=j \omega L_{2} \mathbf{I}_{2}-$ |  |
|  |  | $\begin{aligned} & \mathbf{v}_{1}=\frac{N_{1}}{N_{2}} \mathbf{v}_{2} \\ & \mathbf{I}_{1}=-\frac{N_{2}}{N_{1}} \mathbf{I}_{2} \end{aligned}$ |  |
|  |  | $\begin{aligned} \mathbf{v}_{1} & =-\frac{N_{1}}{N_{2}} \mathbf{v}_{2} \\ \mathbf{l}_{1} & =\frac{N_{2}}{N_{1}} \mathbf{l}_{2} \end{aligned}$ |  |

